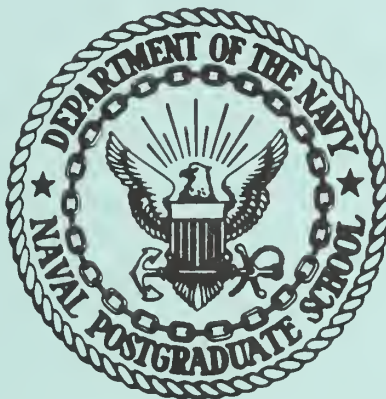


GENERAL CIRCULATION EXPERIMENTS WITH
A TWO-LEVEL QUASI-GEOSTROPHIC MODEL
INCLUDING THE NON-LINEAR INTERACTION
BETWEEN A SINGLE WAVE IN THE ZONAL
DIRECTION AND THE MEAN FLOW

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THESIS

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General Circulation Experiments
With a Two-Level Quasi-Geostrophic Model
Including the Non-Linear Interaction Between
A Single Wave in the Zonal Direction and the Mean Flow

by

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ABSTRACT

A long-period forecast is made utilizing a two-level quasi-geostrophic model. The model includes friction and heating which is a linear function of y . The model was further simplified by restricting the disturbance to one wave in the zonal direction. Experiments were performed with two distances between the walls. In the case of the longer separation, a solution with appreciable time fluctuations was obtained with the largest fluctuation being investigated in more detail. The smaller separation revealed a traveling wave of constant amplitude similar to that observed in certain dishpan experiments.

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TABLE OF SYMBOLS AND ABBREVIATIONS

| | |
|------------|-------------------------------------------------------------------|
| A_v | Vertical eddy viscosity |
| A_H | Horizontal eddy viscosity |
| β_o | Derivative of coriolis parameter at $y = 0$ |
| C_p | Specific heat at constant pressure |
| f_o | Coriolis parameter at $y = 0$ |
| g | Gravity |
| ω | dp/dt |
| Ψ | gz/f_o |
| R | Gas constant |
| ρ | Density |
| \bar{T} | Average temperature from standard atmosphere |
| σ | $(R^2 \bar{T} / p^2 g) (\partial \bar{T} / \partial z + g / C_p)$ |
| ζ | $\nabla^2 \Psi$ |
| z | Height |
| κ | R / C_p |
| Q | Heating added per unit mass |
| ∇^4 | Bi-harmonic operator $(\nabla^2)^2$ |
| W | Distance between the walls |

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I. INTRODUCTION

Knowledge of the general circulation has been made possible with the advent of high-speed large-capacity electronic digital computers. In a classic experiment, Phillips [1956] performed a long-period numerical forecast with a two-level quasi-geostrophic model in a zonally periodic channel on a β plane. Friction and heating were included in his equations with the latter as a linear function of latitude. He introduced a finite amplitude initial disturbance into a baroclinically unstable zonal current. Major deficiencies were the error from the β plane and the geostrophic approximations, the latter making it impossible to account for non-geostrophic dynamics. Furthermore, due to computational errors, he did not achieve a statistically steady state. However, Phillips did initially demonstrate the feasibility of numerical simulation of the atmosphere.

General circulation experiments have progressed in sophistication and complexity since Phillips'. Smagorinsky [1963] formulated a two-level baroclinic primitive equation model by using the Eulerian equations of motion within a spherically zonal strip. Continued sophistication of the experiments resulted in a nine-level model utilizing the primitive equations of motion [Smagorinsky, Manabe and Holloway, 1965]. This study included a resolution of boundary layer fluxes and radiative transfer involving ozone, carbon dioxide and water vapor. A continuation of this study was performed for the tropics which was successful in simulating the tropical convergence zone and the thermal structure [Manabe and Smagorinsky, 1967]. Mintz

[1964] conducted an experiment in which the primitive equations of motion were developed for a two-level model of the atmosphere with the heating and friction terms retained. This model further brought in the effects of land-sea contrasts in heating. Nitta [1967] utilized a twenty-level model for computing vertical distribution of the geopotential flux and conversion of eddy potential energy and eddy kinetic energy due to non-stationary disturbances. A model which has the distinguishing feature of using height rather than pressure was developed [Kasahara and Washington, 1967] and hydrostatic equilibrium was maintained in the system. Some advantages of this model are the prognostic equations have a simpler form than those of the σ system and the lower boundary conditions may be easily formulated. The integration of the nine-level primitive equation model was further extended by the box method [Kurihara and Holloway, 1967] which conserved the conservational properties of the original equations. Recently, the effect of hydrology of the earth's surface was incorporated in the nine-level primitive equation model [Manabe, 1969]. The scheme involved the prediction of water vapor in the atmosphere and the prediction of soil moisture and snow cover. The numerical integrations were performed for the annual mean distribution of solar insolation.

The increased sophistication and complexity of recent models have also produced complex results which make interpretation difficult. Therefore, in this study, the complexities have been kept to a minimum while still maintaining a description of the basic dynamic processes. When the effects of heating and friction are included, the two-level quasi-geostrophic model is the simplest model capable of describing the general circulation.

The model is further simplified in that the disturbance is restricted to a single wave in the zonal direction. Phillips' [1956] experiments and Smagorinsky's [1963] experiment which contained no forcing function in the east-west direction, displayed a single predominate wave number which contained much of the disturbance energy. The y-structure of the disturbance and the mean flow are calculated accurately with a sufficient number of grid points. Some general circulation experiments have been made with even simpler models which represent the y-variation of all quantities with a few terms of a Fourier series [Bryan, 1959; Lorenz, 1962, 1963; Young, 1966]. These models do not provide an adequate description of the barotropic interaction between the disturbance and the mean flow. Consequently, this model appears to be the simplest model which can describe the main mechanisms of the general circulation of the atmosphere.

II. THE FORECAST EQUATIONS

A simple two-level model is constructed by dividing the entire atmosphere into four layers of constant pressure differential, $\frac{\Delta p}{2}$ (fig. 1), numbered 0 to 4 from top to bottom. Assume vertical motion to be zero at the top of the atmosphere, while

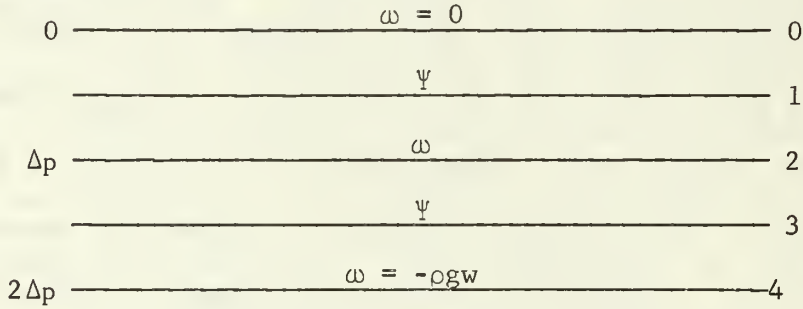


Fig. 1. Two-level model used for prediction .

the vertical motion term at the earth's surface is approximated by

$$\omega \approx -\rho g w_4. \quad (2.1)$$

Charney and Eliassen [1949] used the Ekman theory to derive an expression for w_4 which is

$$w_4 = \frac{1}{2} \left(\frac{2 A_v}{f_o} \right)^{1/2} \sin 2 \alpha \zeta_4, \quad (2.2)$$

where A_v is the vertical eddy viscosity and α , the inflow angle. The surface geostrophic vorticity is approximated by

$$\zeta_4 \approx \zeta_3 = \nabla^2 \psi_3. \quad (2.3)$$

Following the development of Thompson [1961], but with different notation, begin with the quasi-geostrophic vorticity equation

$$\frac{\partial}{\partial t} \nabla^2 \psi + \mathbf{k} \times \nabla \psi \cdot \nabla (\nabla^2 \psi) + \beta_o \frac{\partial \psi}{\partial x} - f_o \frac{\partial \omega}{\partial p} = A_H \nabla^4 \psi. \quad (2.4)$$

Apply this equation at levels 1 and 3 giving

$$\frac{\partial}{\partial t} \nabla^2 \Psi_1 + \mathbf{k} \times \nabla \Psi_1 \cdot \nabla (\nabla^2 \Psi_1) + \beta_o \frac{\partial \Psi_1}{\partial x} - f_o \frac{\omega_2}{\Delta p} = A_H \nabla^4 \Psi_1, \quad (2.5)$$

$$\frac{\partial}{\partial t} \nabla^2 \Psi_3 + \mathbf{k} \times \nabla \Psi_3 \cdot \nabla (\nabla^2 \Psi_3) + \beta_o \frac{\partial \Psi_3}{\partial x} + f_o \frac{(\omega_4 - \omega_2)}{\Delta p} = A_H \nabla^4 \Psi_3. \quad (2.6)$$

If it is desired to stop at some intermediate point, say the tropopause, smaller layers could be utilized rather than to include the entire atmosphere.

Next consider the quasi-geostrophic first law of thermodynamics in the form

$$\frac{\partial}{\partial t} \frac{\partial \Psi}{\partial p} + \mathbf{k} \times \nabla \Psi \cdot \nabla \left(\frac{\partial \Psi}{\partial p} \right) + \frac{\sigma}{f_o} \omega = - \frac{\kappa}{f_o p} Q. \quad (2.7)$$

where

$$\sigma = \frac{R^2 T_s}{2 p g} \left[\frac{\partial T_s}{\partial z} + \frac{g}{C_p} \right]. \quad (2.7a)$$

and T_s is the temperature from the standard atmosphere. When this equation is applied at level 2, the result is

$$\frac{\partial}{\partial t} (\Psi_1 + \Psi_3) + \mathbf{k} \times \nabla \frac{(\Psi_1 + \Psi_3)}{2} \cdot \nabla (\Psi_1 - \Psi_3) - \frac{\Delta p \sigma \omega_2}{f_o} = \frac{\kappa}{f_o} Q_2. \quad (2.8)$$

Define the following quantities

$$\Psi_m = \frac{\Psi_1 + \Psi_3}{2}, \quad (2.9)$$

$$\Psi_T = \frac{\Psi_1 - \Psi_3}{2}, \quad (2.10)$$

which implies

$$\Psi_1 = \Psi_m + \Psi_T, \quad (2.11)$$

$$\Psi_3 = \Psi_m - \Psi_T. \quad (2.12)$$

Here Ψ_T is proportional to the layer thickness and is therefore a measure of the mean temperature. Using these definitions, add (2.5) and (2.6) and divide the result by 2, obtaining

$$\begin{aligned} \frac{\partial}{\partial t} \nabla^2 \Psi_m + k \times \nabla \Psi_m \cdot \nabla (\nabla^2 \Psi_m) + k \times \Psi_T \cdot \nabla (\nabla^2 \Psi_T) + \beta_o \frac{\partial \Psi_m}{\partial x} - f_o \frac{\omega_4}{2 \Delta p} \\ = A_H \nabla^4 \Psi_m. \end{aligned} \quad (2.13)$$

For the second forecast equation, subtract (2.6) from (2.5) and eliminate ω_2 using (2.8)

$$\begin{aligned} \frac{\partial}{\partial t} (\nabla^2 - \mu^2) \Psi_T + k \times \nabla \Psi_m \cdot \nabla (\nabla^2 - \mu^2) \Psi_T + k \times \nabla \Psi_T \cdot \nabla (\nabla^2 \Psi_m) \\ + \beta_o \frac{\partial \Psi_T}{\partial x} + f_o \frac{\omega_4}{2 \Delta p} = - \mu^2 \frac{\kappa Q_2}{2 f_o} + A_H \nabla^4 \Psi_T, \end{aligned} \quad (2.14)$$

where

$$\mu^2 = \frac{2 f_o^2}{\Delta p^2 \sigma}. \quad (2.14a)$$

These are the prediction equations for the model. At this point we restrict ourselves to a disturbance of wave number k and the mean flow. The fields may be defined as follows

$$\Psi_m = E(y,t) + A(y,t) \cos kx + B(y,t) \sin kx, \quad (2.15)$$

$$\Psi_T = F(y,t) + C(y,t) \cos kx + D(y,t) \sin kx, \quad (2.16)$$

where k is the x wave number, A through D are Fourier amplitudes of the disturbance and E and F are the zonal mean fields. Now substitute expressions for Ψ_m and Ψ_T into (2.13), separate the various terms, neglecting all terms with wave number $2k$ or higher. Equating coefficients of the cosine terms gives

$$\begin{aligned} \frac{\partial}{\partial t} \left(\frac{\partial^2 A}{\partial y^2} - A k^2 \right) = k \left[\frac{\partial E}{\partial y} \frac{\partial^2 B}{\partial y^2} + \frac{\partial F}{\partial y} \frac{\partial^2 D}{\partial y^2} - \frac{\partial^3 E}{\partial y^3} B - \frac{\partial^3 F}{\partial y^3} D - \right. \\ \left. k^2 \left(\frac{\partial E}{\partial y} B + \frac{\partial F}{\partial y} D \right) \right] - \beta_o B k - K \left(\frac{\partial^2}{\partial y^2} - k^2 \right) (A - C) + \\ A_H \left[\frac{\partial^4 A}{\partial y^4} - 2k^2 \frac{\partial^2 A}{\partial y^2} + k^4 A \right]. \end{aligned} \quad (2.17)$$

For the sine terms the result is

$$\begin{aligned} \frac{\partial}{\partial t} \left(\frac{\partial^2 B}{\partial y^2} - Bk^2 \right) = k \left[- \frac{\partial E}{\partial y} \frac{\partial^2 A}{\partial y^2} - \frac{\partial F}{\partial y} \frac{\partial^2 C}{\partial y^2} + \frac{\partial^3 E}{\partial y^3} A + \frac{\partial^3 F}{\partial y^3} C + \right. \\ \left. k^2 \left(\frac{\partial E}{\partial y} A + \frac{\partial F}{\partial y} C \right) \right] + \beta_o Ak - K \left(\frac{\partial^2}{\partial y^2} - k^2 \right) (B-D) + \\ A_H \left[\frac{\partial^4 B}{\partial y^4} - 2k^2 \frac{\partial^2 B}{\partial y^2} - k^4 B \right]. \end{aligned} \quad (2.18)$$

Repeating the procedures for (2.14), the equations are

$$\begin{aligned} \frac{\partial}{\partial t} \left(\frac{\partial^2 C}{\partial y^2} - Ck^2 - C\mu^2 \right) = k \left[\frac{\partial E}{\partial y} \frac{\partial^2 D}{\partial y^2} + \frac{\partial F}{\partial y} \frac{\partial^2 B}{\partial y^2} - \frac{\partial E}{\partial y} D (k^2 + \mu^2) - \right. \\ \left. \frac{\partial F}{\partial y} B (k^2 - \mu^2) - \frac{\partial^3 E}{\partial y^3} D - \frac{\partial^3 F}{\partial y^3} B \right] - \beta_o Dk + \\ K \left(\frac{\partial^2}{\partial y^2} - k^2 \right) (A-C) + \\ A_H \left[\frac{\partial^4 C}{\partial y^4} - 2k^2 \frac{\partial^2 C}{\partial y^2} + k^4 C \right], \end{aligned} \quad (2.19)$$

and

$$\begin{aligned} \frac{\partial}{\partial t} \left(\frac{\partial^2 D}{\partial y^2} - Dk^2 - D\mu^2 \right) = k \left[\frac{\partial E}{\partial y} C (k^2 + \mu^2) + \frac{\partial F}{\partial y} A (k^2 - \mu^2) - \right. \\ \left. \frac{\partial E}{\partial y} \frac{\partial^2 C}{\partial y^2} - \frac{\partial F}{\partial y} \frac{\partial^2 A}{\partial y^2} + \frac{\partial^3 F}{\partial y^3} A + \frac{\partial^3 E}{\partial y^3} C \right] + \\ \beta_o Ck + K \left(\frac{\partial^2}{\partial y^2} - k^2 \right) (B-D) + \\ A_H \left[\frac{\partial^4 D}{\partial y^4} - 2k^2 \frac{\partial^2 D}{\partial y^2} + k^4 D \right]. \end{aligned} \quad (2.20)$$

Equating coefficients of terms independent of x in (2.13) gives

$$\begin{aligned} \frac{\partial}{\partial t} \frac{\partial^2 E}{\partial y^2} = \frac{k}{2} \frac{\partial}{\partial y} \left[A \frac{\partial^2 B}{\partial y^2} - B \frac{\partial^2 A}{\partial y^2} + C \frac{\partial^2 D}{\partial y^2} - D \frac{\partial^2 C}{\partial y^2} \right] - \\ K \frac{\partial}{\partial y} \left(\frac{\partial E}{\partial y} - \frac{\partial F}{\partial y} \right) + A_H \frac{\partial}{\partial y} \left(\frac{\partial^3 E}{\partial y^3} \right). \end{aligned} \quad (2.21)$$

Similarly, coefficients independent of x in (2.14) results in

$$\begin{aligned} \left(\frac{\partial^2}{\partial y^2} - \mu^2 \right) \frac{\partial F}{\partial y} = \frac{k}{2} \frac{\partial}{\partial y} \left[A \frac{\partial^2 D}{\partial y^2} - B \frac{\partial^2 C}{\partial y^2} + C \frac{\partial^2 B}{\partial y^2} - D \frac{\partial^2 A}{\partial y^2} + \right. \\ \left. \mu^2 \left(B \frac{\partial C}{\partial y} + C \frac{\partial B}{\partial y} - A \frac{\partial D}{\partial y} - D \frac{\partial A}{\partial y} \right) \right] + \\ K \left(\frac{\partial E}{\partial y} - \frac{\partial F}{\partial y} \right) - \frac{\mu^2 \kappa Q_2}{2} + A_H \frac{\partial}{\partial y} \left(\frac{\partial^3 F}{\partial y^3} \right), \end{aligned} \quad (2.22)$$

where

$$K = \frac{f_o g}{2RT} \left(\frac{A_m}{f_o} \right)^{1/2}. \quad (2.23)$$

The prediction equations are now in the form to be used in the model.

III. FINITE DIFFERENCE SCHEME AND BOUNDARY CONDITIONS

The finite difference scheme used is illustrated below with a sample variable N ;

$$\frac{\partial N}{\partial y} = \frac{1}{2H} (N_{i+1} - N_{i-1}) \quad (3.1)$$

$$\frac{\partial^2 N}{\partial y^2} = \frac{1}{H^2} (N_{i+1} - 2N_i + N_{i-1}) \quad (3.2)$$

$$\frac{\partial^3 N}{\partial y^3} = \frac{1}{2H^3} [(N_{i+2} - 2N_{i+1} + N_i) - (N_i - 2N_{i-1} + N_{i-2})] \quad (3.3)$$

where i is the grid index and H the distance between grid points.

Centered time differences are used for all quantities except those involving friction. The frictional terms are computed at time $(t-\Delta t)$. In all cases the first step was a forward time step. A special time step was introduced every 24 time steps to avoid the separation of solutions at even and odd time steps. These special time steps used the backwards difference method utilized by Matsuno [1966]. Second order equations (2.17), (2.18), (2.19) and (2.20) for time tendencies are solved by the exact method of Richtmyer [1957]. A modification of the Richtmyer method used by Phillips [1956] was necessary for equation (2.22) to satisfy the boundary conditions. Equation (2.21) was solved by a direct marching process utilizing the boundary conditions.

The following boundary conditions were established:

The quantities A through $D = 0$

$$\frac{\partial}{\partial t} \frac{\partial F}{\partial y} = 0 \text{ and } \frac{\partial}{\partial t} \frac{\partial E}{\partial y} = 0 \quad \text{all at } y = 0 \text{ and } y = W.$$

Following Phillips [1956] the mean and disturbance vorticity are set equal to zero at the boundary in order to make the boundary walls smooth.

IV. INITIAL CONDITIONS

A natural initial state would be one of constant temperature and no motion. The heating, in time, would build up a baroclinic current. No disturbance could develop until the vertical shear of the zonal current reached a critical value. In order to save computer time, the initial state was chosen to consist of a zonal current with a vertical shear near the critical value [see Thompson, 1961]. The initial disturbance has a wave length and a y-structure such that when superimposed on a baroclinic current with no horizontal shear it would have maximum growth rate.

The initial conditions for the model are

$$A = 200 \sin \frac{\pi y}{W}$$

$$B \text{ through } D = 0$$

$$F = \frac{f_o HW_6}{\pi} \cos \frac{\pi y}{W}$$

$$E = \frac{f_o HW_6}{\pi} \cos \frac{\pi y}{W} .$$

V. RESULTS

The main experiments were conducted using the physical parameters listed in Table I.

| |
|-----------------------------------------------------------------------|
| $f_o = 1 \times 10^{-4}$ per second |
| $\sigma = 2.3$ meters squared per second squared per centibar squared |
| $\beta = 1.67 \times 10^{-11}$ per meter per second |
| $\Delta p = 50$ centibars |
| $A_v = 40$ meters squared per second |
| $A_H = 1 \times 10^5$ meters squared per second |
| $\alpha = 22.5$ degrees |
| $\mu^2 = 2.49 \times 10^{-12}$ per meter squared |
| $H = 200$ kilometers |
| $\Delta t = 0.5$ hours |
| $k = 2\pi/4000$ per kilometer |

Table I - Numerical Values of the Physical Constants

The variation of experiments 2 and 3 from the main experiment is tabulated in Table II.

| | W (Km) | Q (Kj per ton per sec) |
|--------------|--------|-------------------------------------------------------|
| Experiment 1 | 8000 | $4 \times 10^{-3} \left(y - \frac{W}{2} \right) / W$ |
| Experiment 2 | 8000 | $8 \times 10^{-3} \left(y - \frac{W}{2} \right) / W$ |
| Experiment 3 | 4000 | $8 \times 10^{-3} \left(y - \frac{W}{2} \right) / W$ |

Table II - Variation of the Physical Parameters

The forecast period for all three experiments was 300 days. Figure 2 depicts a plot of the disturbance energy for the 300 day forecast period. The disturbance energy referred to throughout the discussion is defined in Appendix C (Eqs. C-10 and C-11). A main feature of Fig. 2 is that the disturbance energy does not reach a steady state although it appears to be statistically stable after the first 120 days.

Figure 3 displays a time section of the mean wind for the period 120-260 days which is the main time period of interest for this experiment. The general increase of the disturbance energy begins to level off near day 140 which corresponds to the initial appearance of the southern jet. This result is similar to observations of Riehl, Yeh and LaSeur [1950]. The period between day 190 and day 200 is of considerable interest. The disturbance energy has its greatest fluctuations during this period and it corresponds to the termination of the southern jet.

Figures 4 - 7 represent the amplitudes and phases of Ψ_m , Ψ_T and w_2 in the form $P\cos(kx-\delta)$ where P is the amplitude and δ is the phase. Figures 4 and 5 represent day 190, prior to the disturbance peak, and Figs. 6 and 7 correspond to day 196, after the peak. The necessary condition for barotropic instability is that $\beta - \frac{\partial^2 \Psi_1}{\partial y^2}$ change sign somewhere in the region [Kuo, 1949]. Calculation at day 190 showed that this condition was satisfied in the vicinity of the southern jet. It is seen in the lower portion of Fig. 4, between $y = 1000$ km and $y = 2500$ km, that the phase tilts of Ψ_m , Ψ_T and w_2 are opposite to the shear of \bar{u}_1 . These phase relationships indicate barotropic amplification and therefore a transformation of energy from the mean flow to the disturbance. However, the northern portion of Fig. 4 shows the

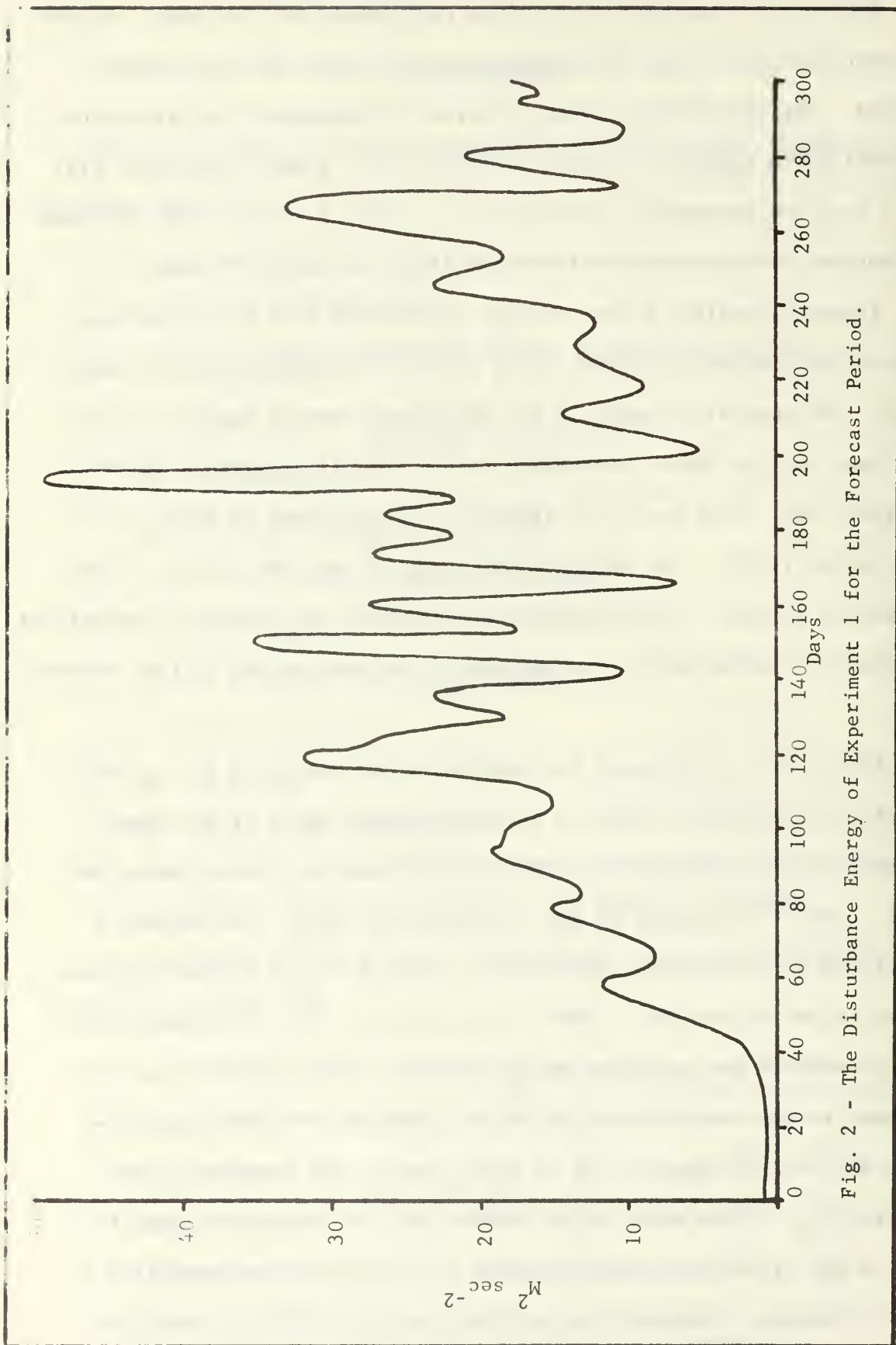


Fig. 2 - The Disturbance Energy of Experiment 1 for the Forecast Period.

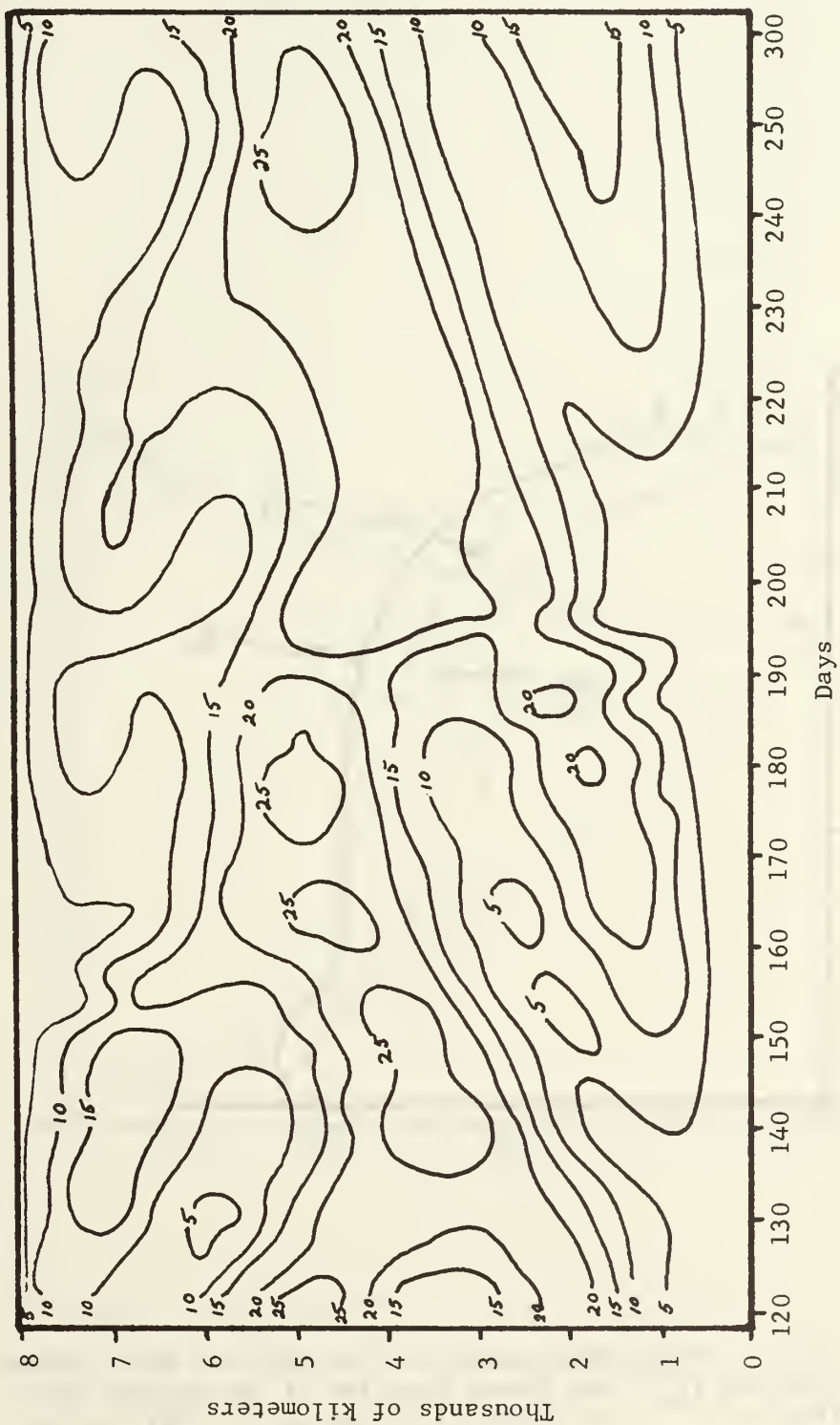


Fig. 3 - Time Cross Section of the Mean Zonal Wind at Level 1.

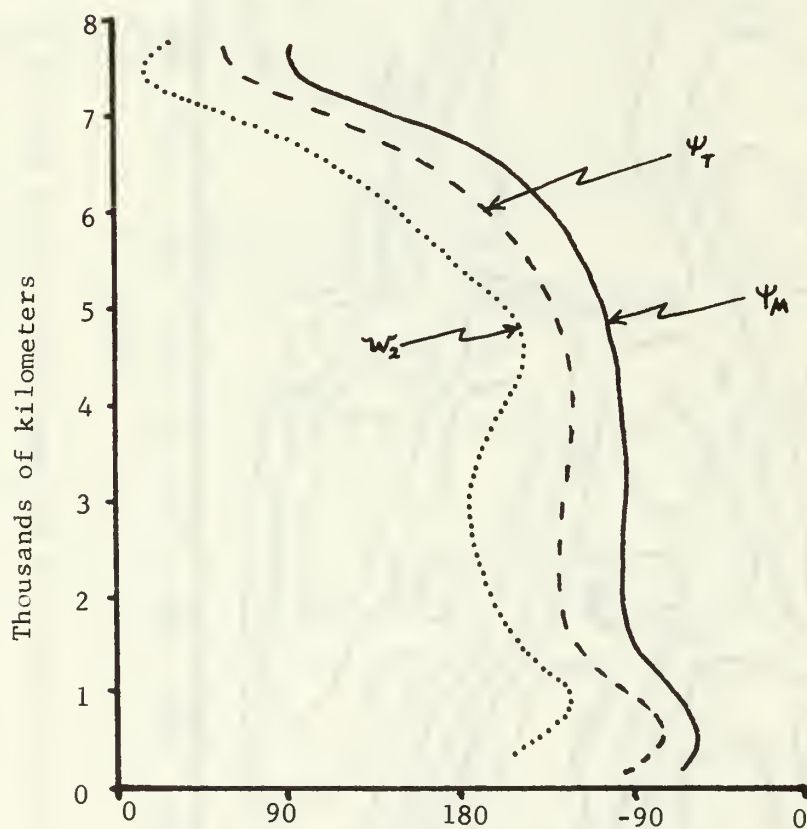


Fig. 4 - Phase Relationship of the Vertical Mean Stream Function (Ψ_m), the Stream Function of the Thermal Wind (Ψ_T) and the Vertical Motion ($w_2 = -\frac{\omega_2}{\rho g}$) for day 190.

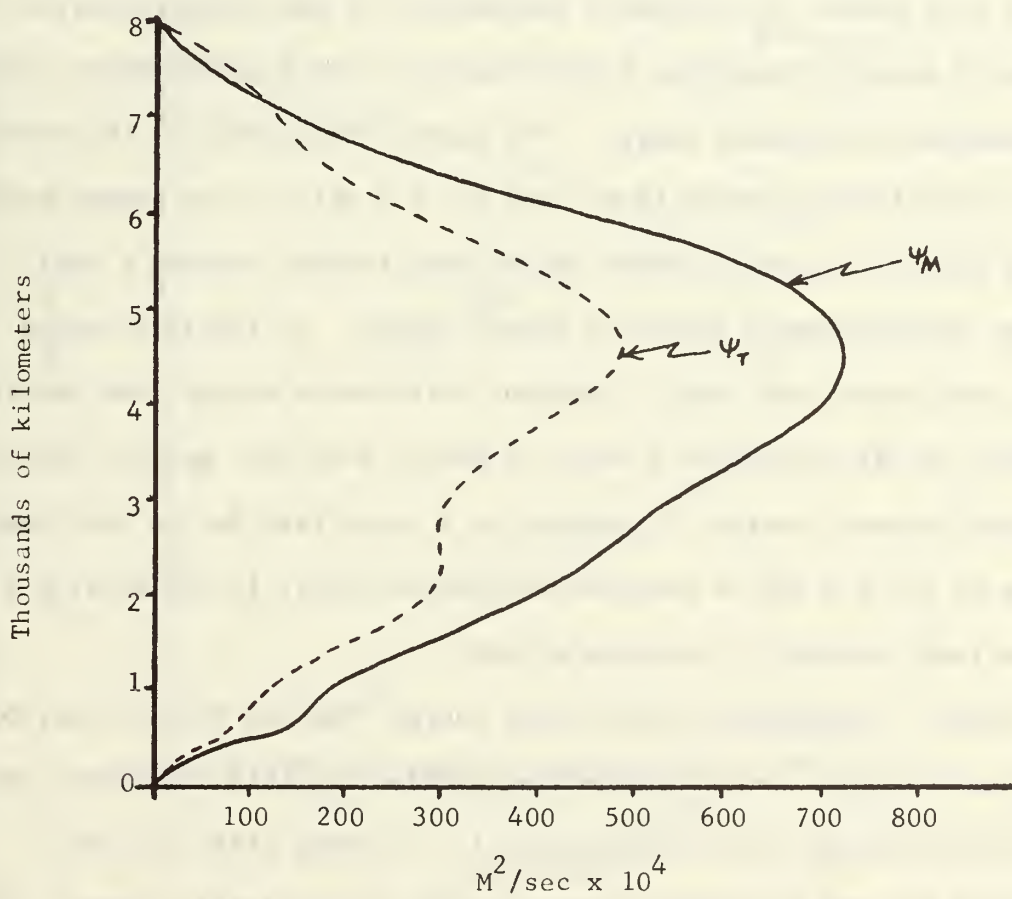


Fig. 5 - Amplitude of ψ_m and ψ_T for day 190.

same tilt as the shear of \bar{u}_1 which indicates barotropic damping: this implies an energy transformation of disturbance kinetic energy to mean kinetic energy. Figure 5 portrays the amplitude of Ψ_m and Ψ_T ; clearly Ψ_m is larger and both fields have a mid-latitude maximum. A secondary peak of amplitude in Ψ_T is beginning to form which is a product of the barotropic instability. Figure 6 shows that all parameters (Ψ_m , Ψ_T , w_2) have a phase tilt which indicates barotropic damping over the entire range. The amplitude of Ψ_m and Ψ_T corresponding to Fig. 6 are displayed in Fig. 7. Of primary note is the distinct double maximum of amplitude which is a result of barotropic instability in the southern region. Figure 8 depicts the energy transformations over a period which includes the maximum disturbance energy. The first item of note is the nearly exact correlation between $[\bar{P} \cdot P']$ and $[P' \cdot K']$ which in an energy balance would almost completely offset one another thereby leaving a small amount of disturbance potential energy change. It should be noted that just before the event of maximum disturbance energy, the barotropic damping $[K' \cdot \bar{K}]$ approached a value of zero. This fact permits the disturbance kinetic energy to increase at a rapid rate due to the large value of $[P' \cdot K']$ and to continue to increase until $[K' \cdot \bar{K}]$ attains a value large enough to terminate growth.

Figure 9 depicts the disturbance energy over the forecast period for experiment 2. As stated earlier (Table II), this experiment has twice the heating rate of experiment 1. A steady state was not attained but the disturbance energy became statistically steady. The main differences from experiment 1 are that the disturbance energy fluctuates more rapidly and that its magnitude is much higher.

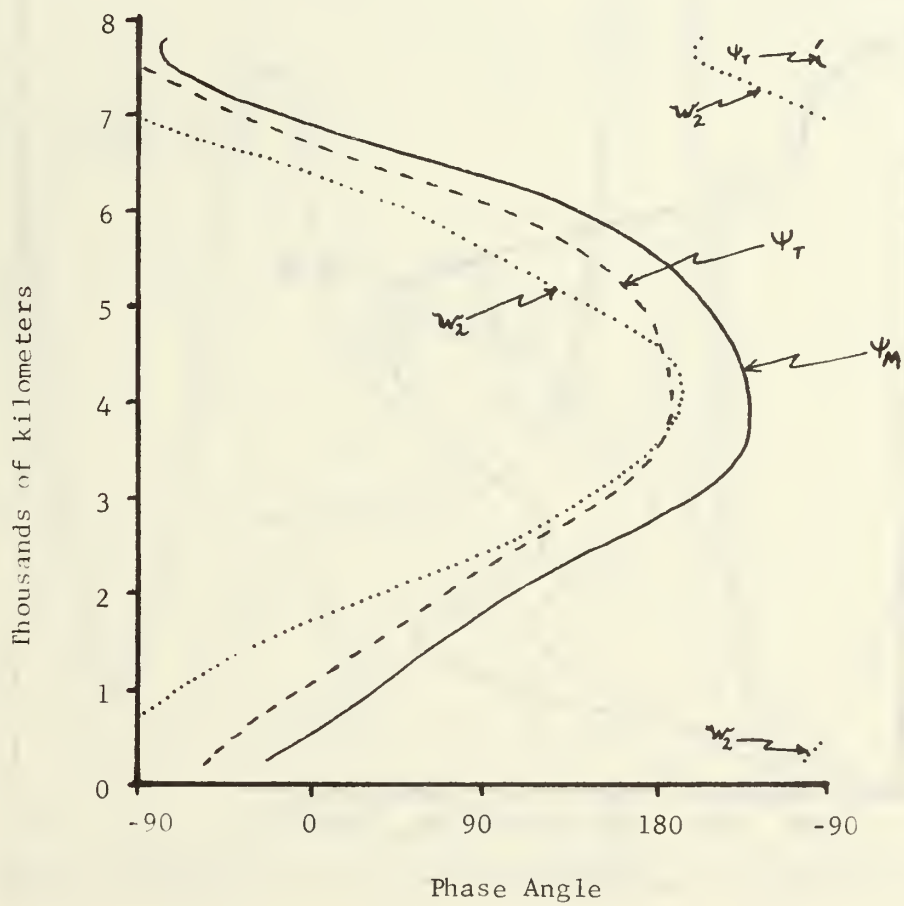


Fig. 6 - Phase Relationship of Ψ_m , Ψ_T and w_2 for day 196.

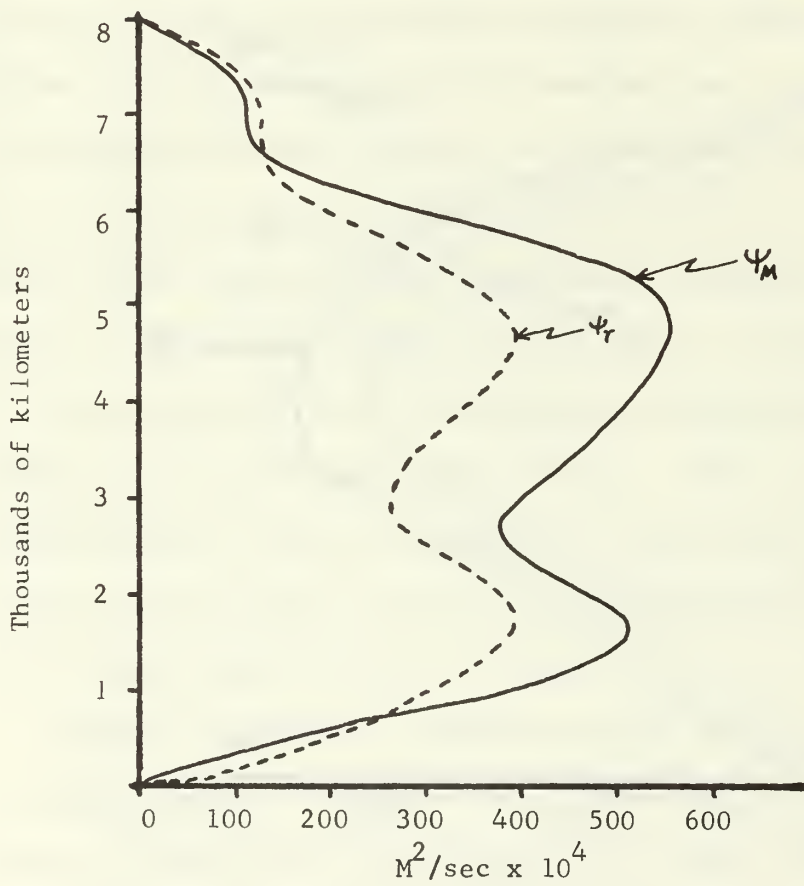


Fig. 7 - Amplitude of Ψ_m and Ψ_T for day 196.

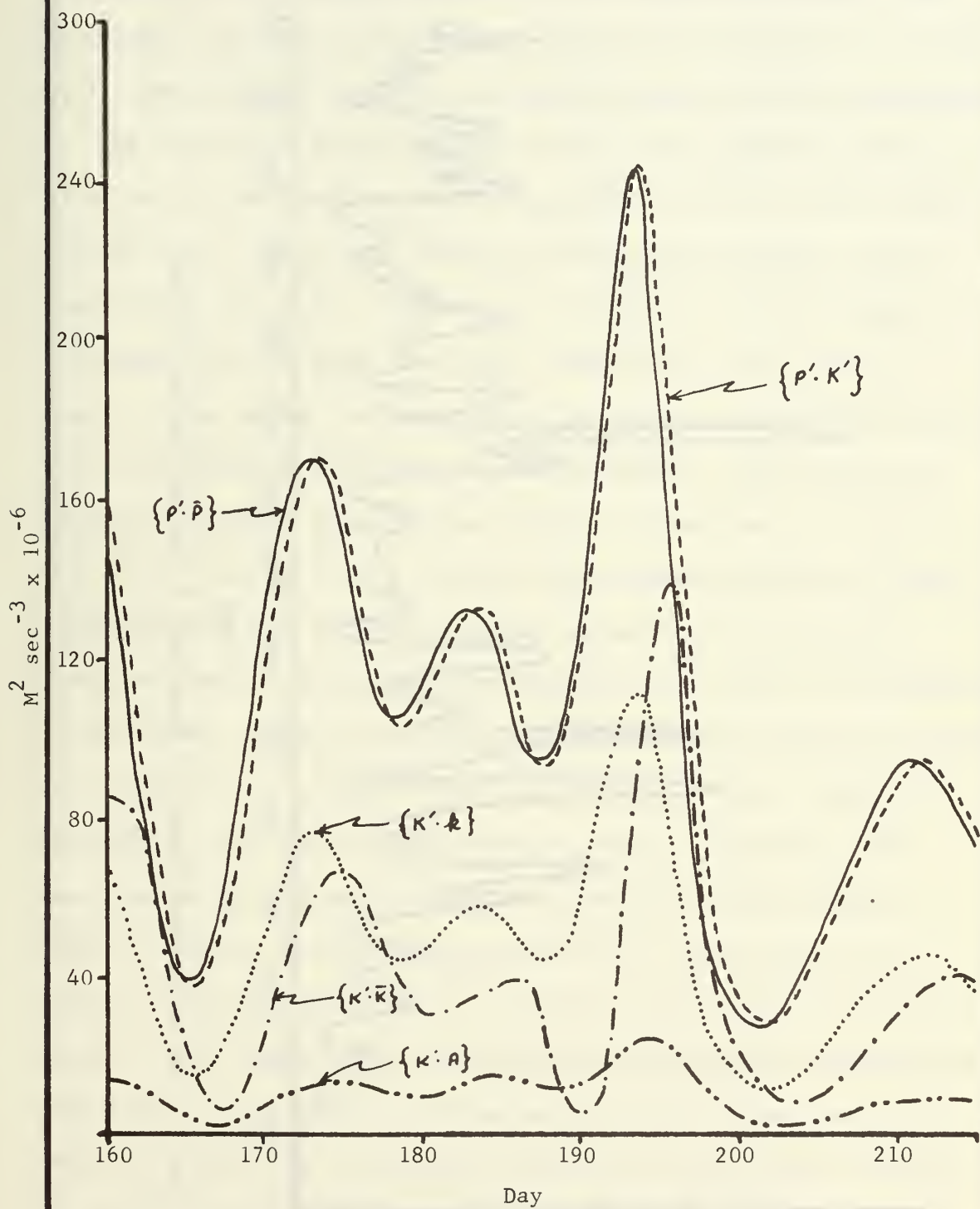


Fig. 8 - Energy Transformation for Period which Includes the Event of Maximum Disturbance.

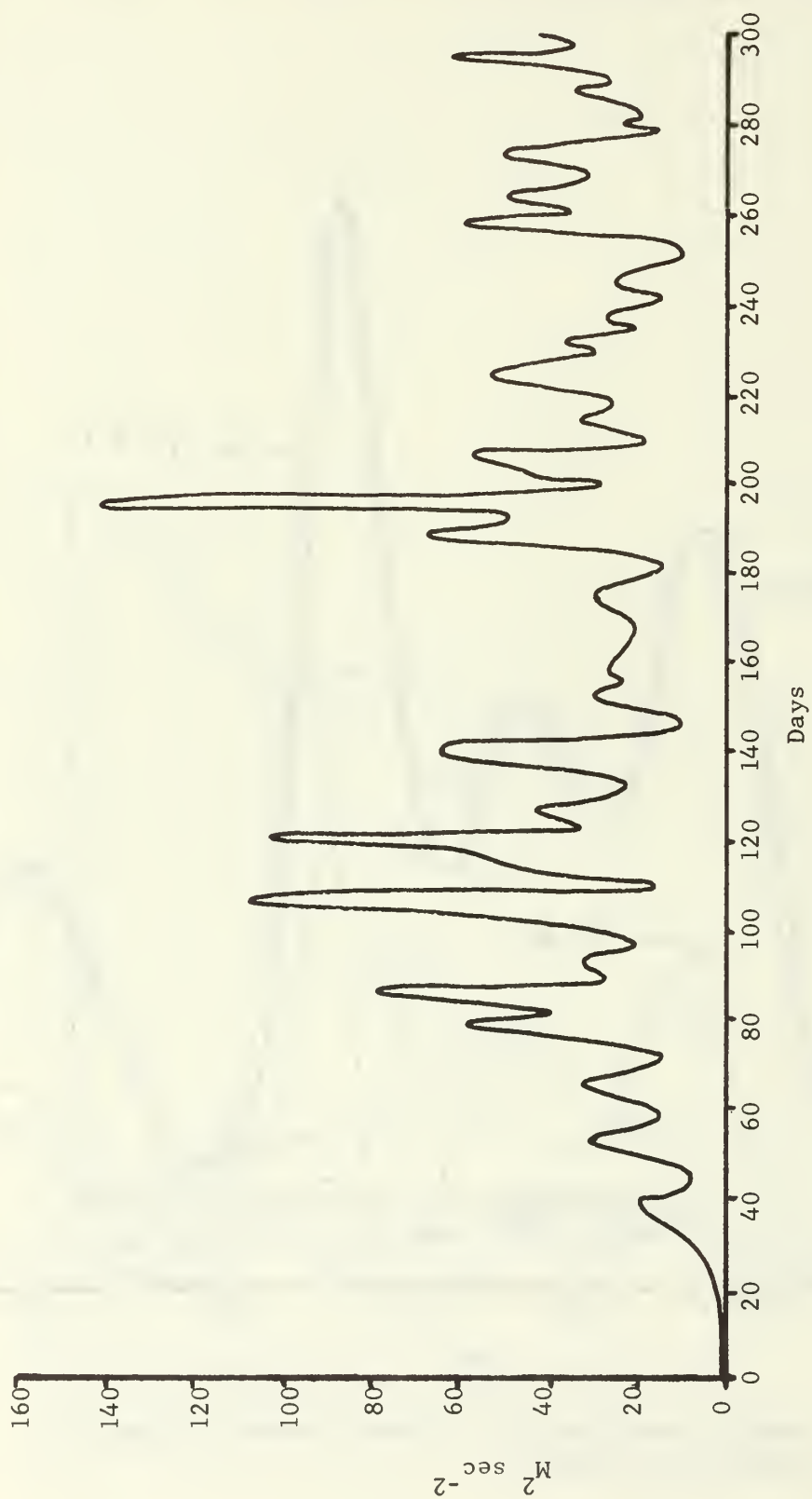


Fig. 9 - The Disturbance Energy of Experiment 2 for the Forecast Period.

A depiction of the disturbance energy over the forecast period for experiment 3 is contained in Fig. 10. This experiment differs from experiment 1 in that the disturbance between the walls has been cut in half. The heating coefficient was doubled from its value in experiment 1. The disturbance energy reached a steady state condition shortly after day 120 and stayed relatively constant to the end of the period. Thus we have a single wave traveling through the atmosphere with no variation in amplitude. This result is similar to certain dishpan experiments with an inner core [Hide, 1953; Fultz, et al, 1959].

Figure 11 represents the phases of ψ_m , ψ_T and w_2 at day 200 and reveals that the parameters have similar phase variations. The phase tilts indicate barotropic damping since there is a single jet in \bar{u}_1 (see Fig. 13). Since ψ_T lags ψ_m , there is a northward heat flux and energy transformation from the mean potential energy to the disturbance potential energy. The correlation mentioned above gives a transformation of disturbance potential energy to disturbance kinetic energy since there is a tendency for cold air to sink and warm air to rise. Figure 12 represents a plot of the amplitudes of ψ_m and ψ_T at day 200. The amplitude of ψ_m is greater than ψ_T and both have a single maximum.

Figure 13 depicts the relationship between \bar{u}_3 , which could be considered the surface wind, and \bar{u}_1 at day 200. This mean wind field is similar to that observed in the atmosphere, although the gradients are much less. At the surface, \bar{u} is westerly in the mid latitudes and easterly at high and low latitudes while at the upper levels the flow is westerly with a mid-latitude jet. Figure 14 is a plot of the

amplitude of the mean meridional component of the wind (\bar{v}_1) for day 200. The amplitude of \bar{v}_1 reveals a northerly component at mid latitudes and a southerly component at high and low latitudes which implies an indirect Ferrel circulation at mid latitudes and a direct Hadley circulation at high and low latitudes.

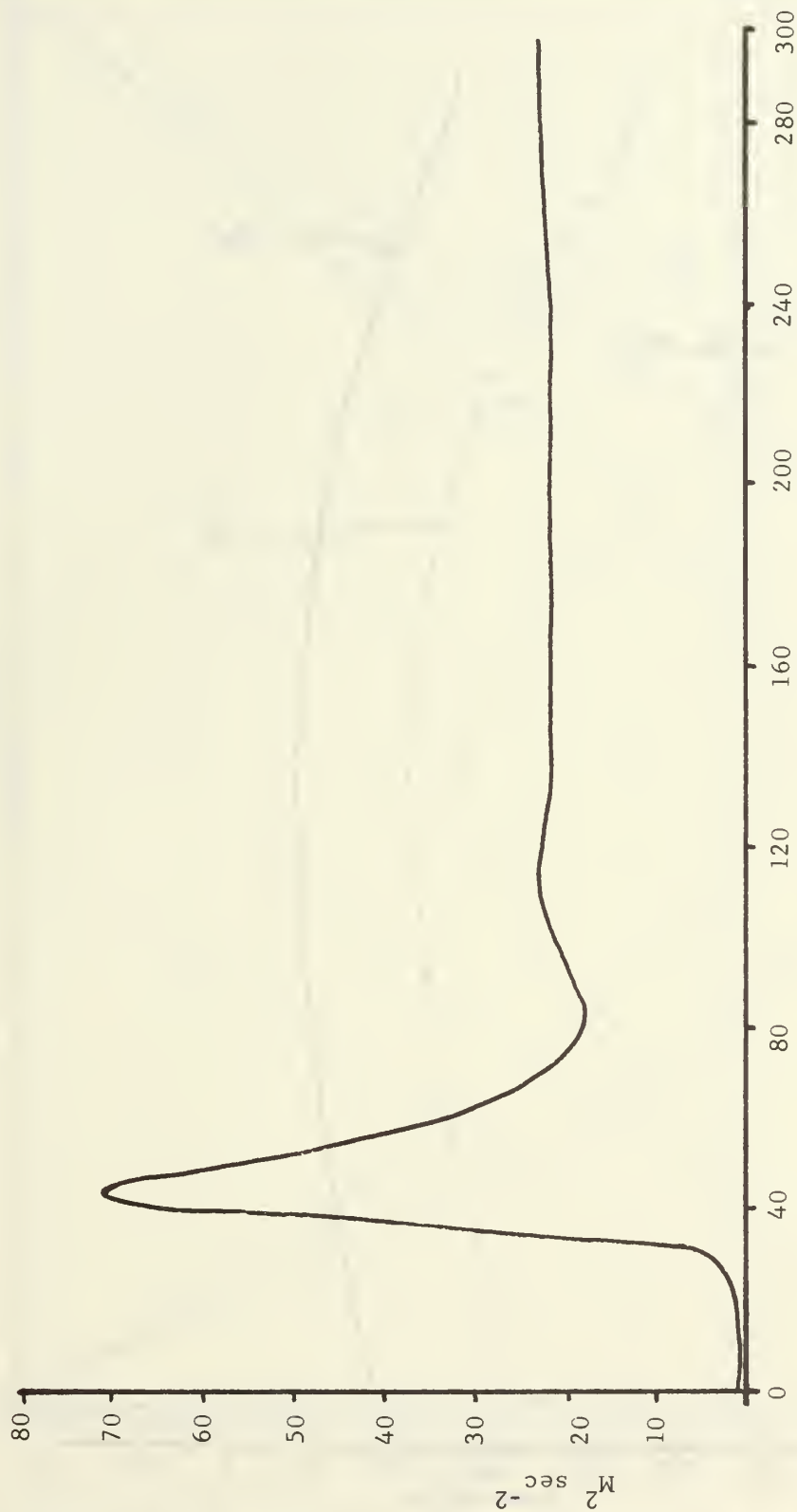


Fig. 10 - The Disturbance Energy for Experiment 3 for the Forecast Period.

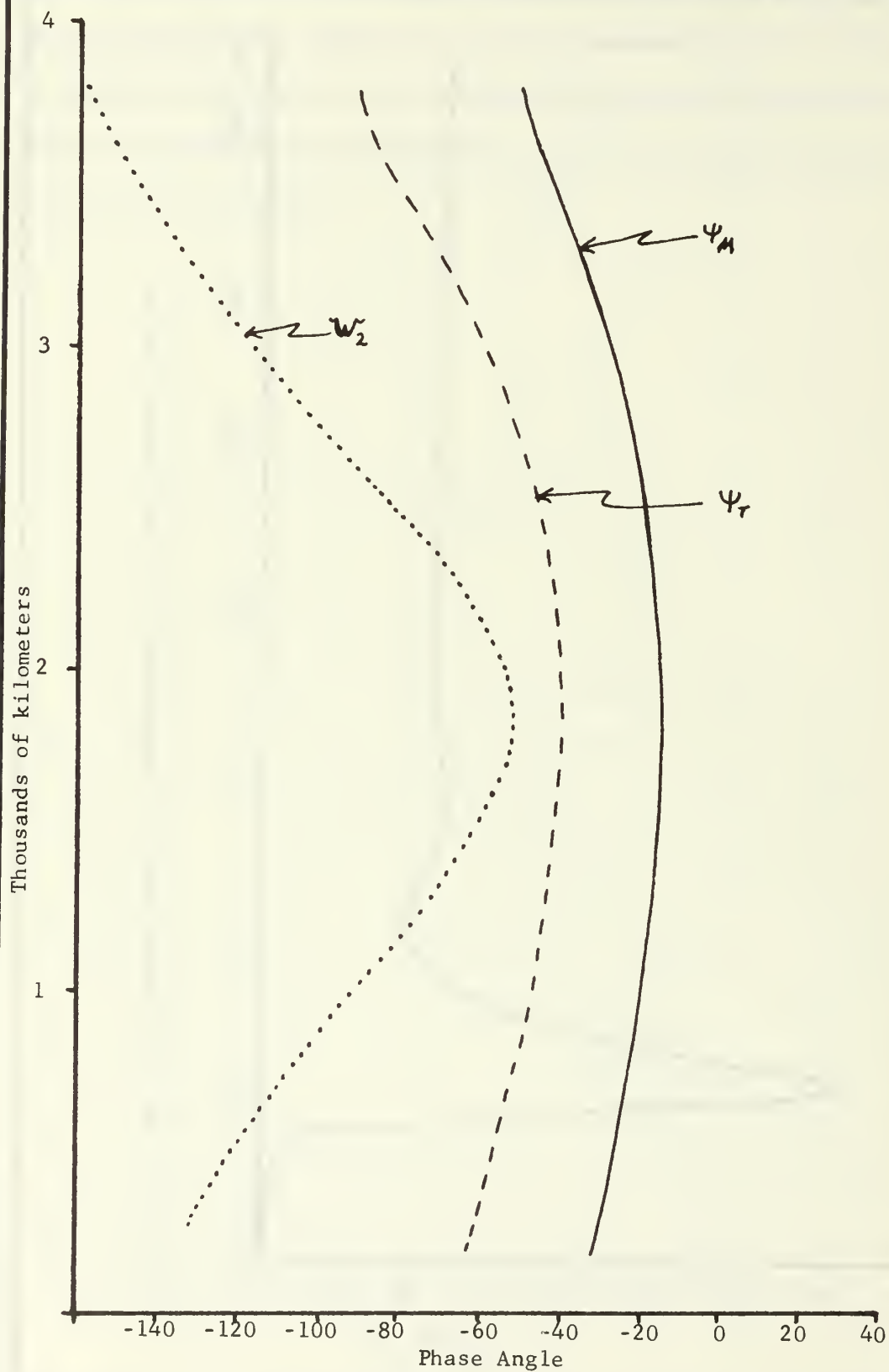
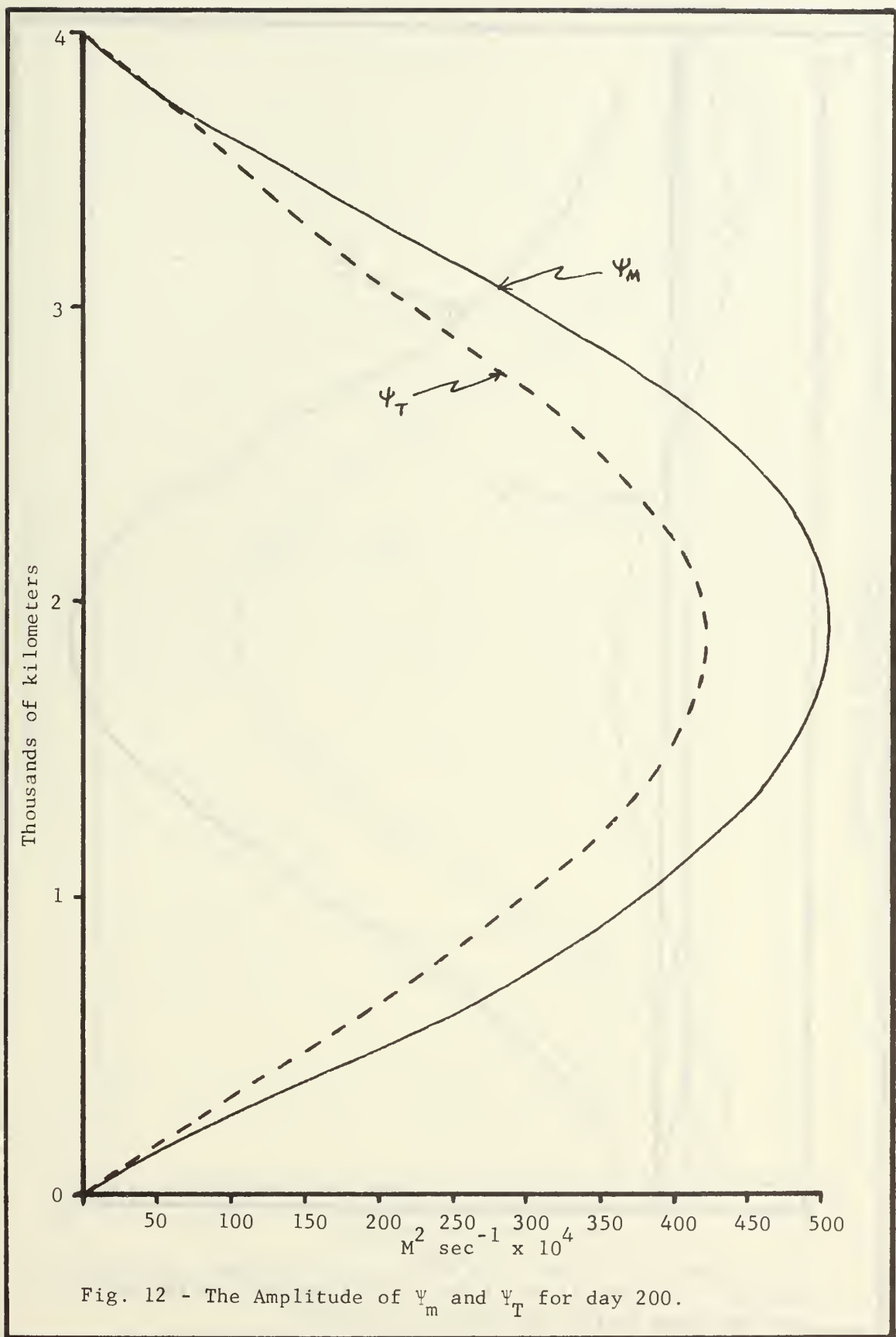


Fig. 11 - The Phase Relationship of ψ_m , ψ_T and w_2 for day 200.



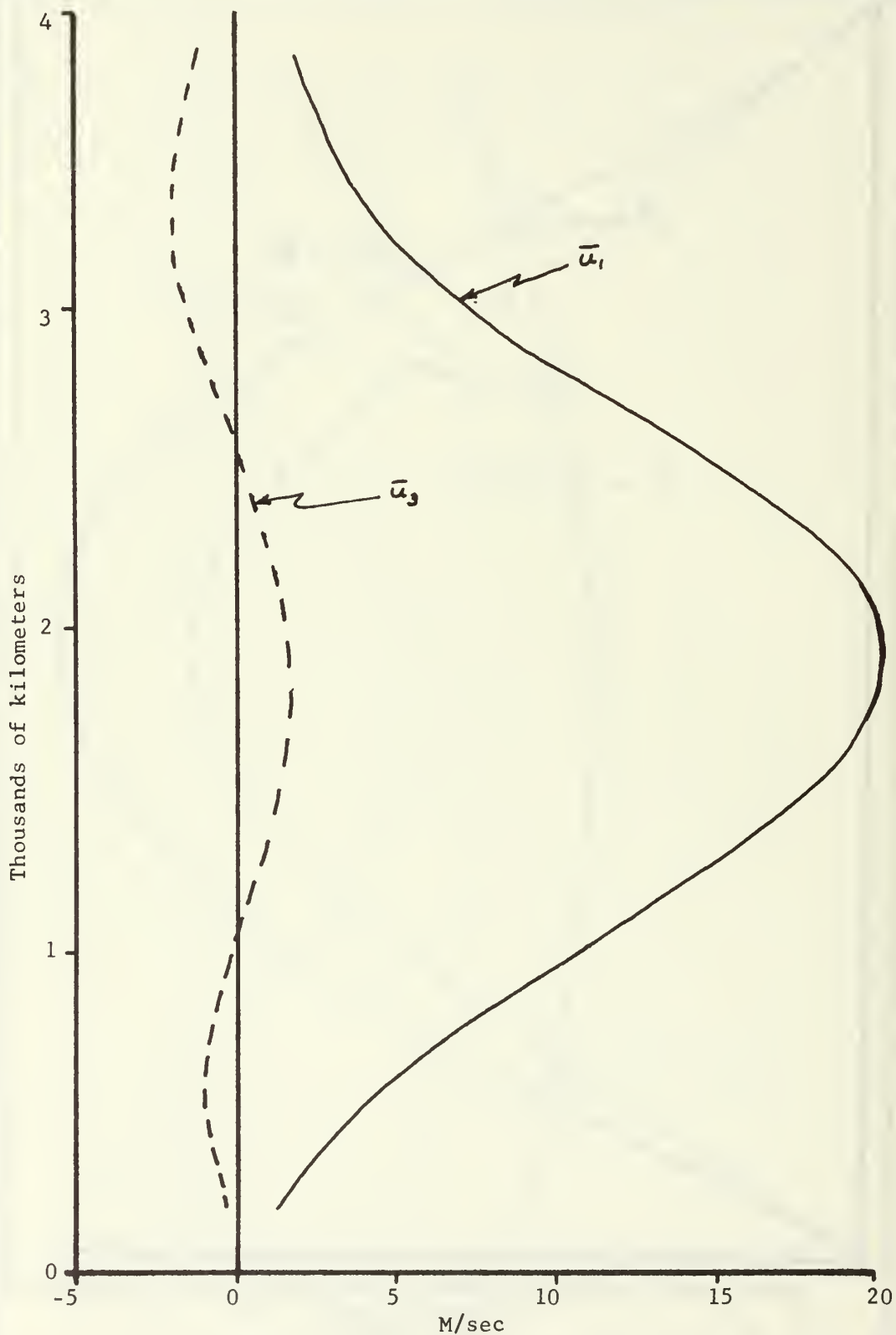


Fig. 13 - The Amplitude of the Zonal Component of the mean (\bar{u}_1) and the Mean Surface Wind (\bar{u}_3) for day 200.

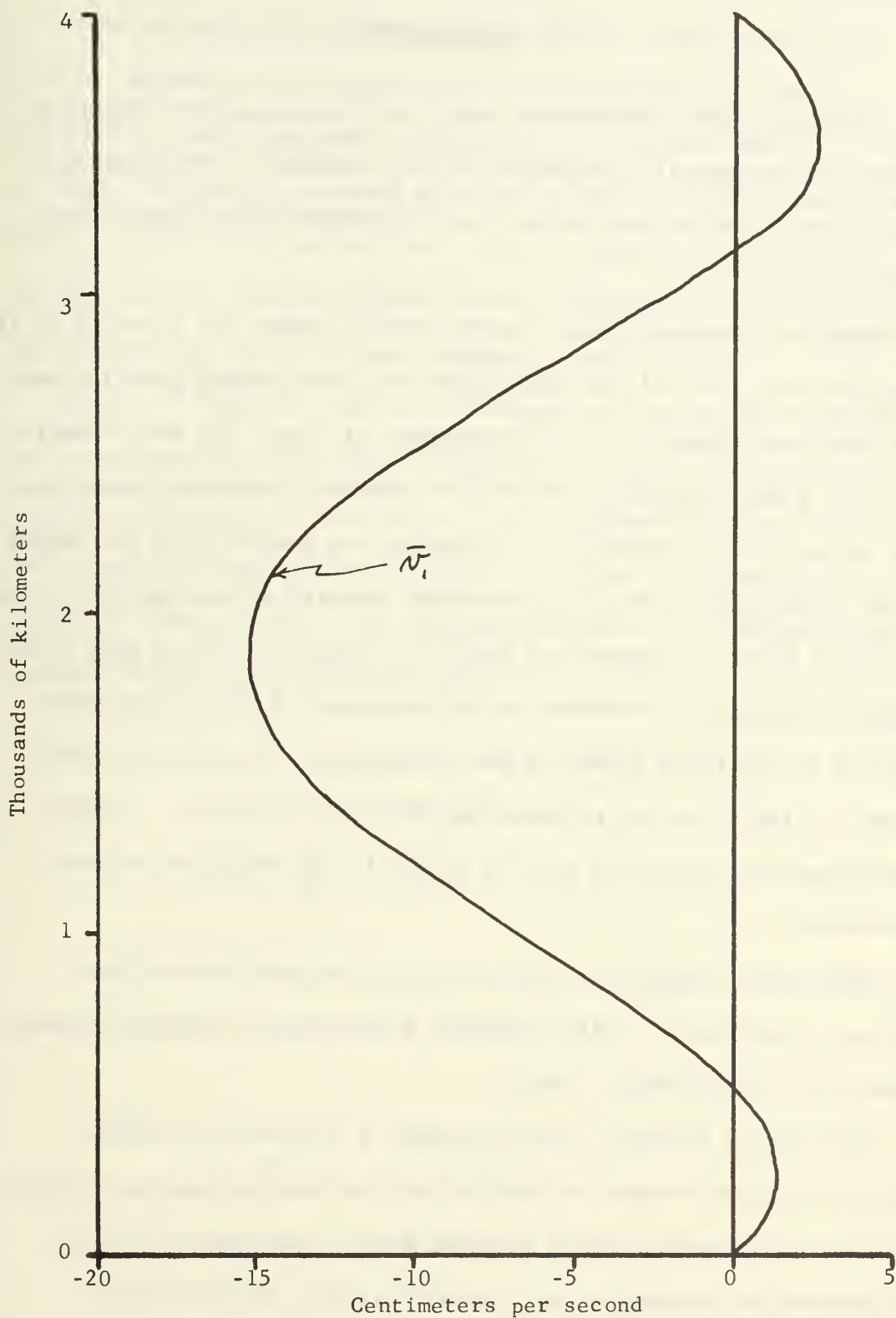


Fig. 14 - The Amplitude of the Mean Meridional Component of the Wind (\bar{v}_1) for day 200.

VI. CONCLUSIONS

A two-level quasi-geostrophic model was formulated for simplified studies of the general circulation of the atmosphere. The model was further simplified by restricting the disturbance to one wave in the zonal direction.

Numerical integration was computationally stable for a period of at least 300 days. In all the experiments the same heating function was used which was linear in y and independent of time. The main experiment with a wall separation of 8000 km produced fluctuating solutions with irregular time variations. Attention was focused on a sub period of the integration where the disturbance featured a rapid growth followed by a rapid decay. Apparently a double jet structure in the mean flow became barotropically unstable at the beginning of the period which resulted in the rapid growth of the disturbance. By the end of the period, a single jet had replaced the double jet structure. Energy transformations verify the roll of $[K' \cdot \bar{K}]$ in the evolution of this disturbance.

Experiment 2 featured a double heating rate and results were similar to experiment 1 with increased fluctuations and higher energy values of the disturbance energy.

Experiment 3 differed from experiment 1 in that the distance between walls was reduced to 4000 km and the heating rate was doubled. The disturbance energy became constant after approximately 120 days and remained so throughout the forecast period. This situation represents a wave of constant amplitude propagating through the

atmosphere. The behavior resembles the flow observed in certain dishpan experiments which contained a central core [Hide, 1953; Fultz, et al, 1959]. Apparently the explanation of the difference in behavior between experiment 1 and experiment 3 is related to the fact that for $W = 8000$ km, at least two energy producing modes of disturbance energy can exist in y , whereas for $W = 4000$ km only one energy producing mode can exist. The presence of two energy producing modes apparently leads to fluctuations in time but the one modal case produces a steady wave.

Further studies utilizing this simple model could be performed such as longer period forecasting; changes in the form of heating; simulating dishpan experiments by setting $\beta = 0$ and concentrating the heating near the boundaries, and a change in the wave number k to name a few. Any or all of these studies could further enhance our understanding of the general circulation of the atmosphere.

APPENDIX A - COMPUTATION OF VERTICAL MOTION

The computation of vertical motion (ω_2) is necessary for the energy equation. To derive the computational equation for vertical motion, start with

$$\omega_2 = \frac{2}{\Delta p \sigma} \left[\frac{\partial \psi_T}{\partial t} + u_m \frac{\partial \psi_T}{\partial x} + v_m \frac{\partial \psi_T}{\partial y} + \frac{\kappa Q_2}{2} \right], \quad (A-1)$$

where

$$u_m = - \frac{1}{f_o} \frac{\partial \psi_m}{\partial y} \quad (A-2)$$

$$v_m = \frac{1}{f_o} \frac{\partial \psi_m}{\partial x} . \quad (A-3)$$

Substituting equations (A-2), (A-3), (2.15) and (2.16) into (A-1), collecting terms, and again neglecting terms with wave number $2k$ or higher results in

$$\begin{aligned} \omega_2 = \frac{2}{\Delta p \sigma} \left\{ \cos kx \left[\frac{\partial C}{\partial t} - \frac{k}{f_o} \left(\frac{\partial E}{\partial y} D - \frac{\partial F}{\partial y} B \right) \right] + \right. \\ \left. \sin kx \left[\frac{\partial D}{\partial t} + \frac{k}{f_o} \left(\frac{\partial E}{\partial y} C - \frac{\partial F}{\partial y} A \right) \right] + \frac{\partial F}{\partial t} + \frac{\kappa Q_2}{2} \right\} . \quad (A-4) \end{aligned}$$

Both the disturbance and the average vertical motion are given by this equation, which is the equation used in the model for the computation of vertical motion.

APPENDIX B - COMPUTATION OF AVERAGE NORTH-SOUTH WIND

The computation of the average north-south wind (\bar{v}_1) is necessary for the energy calculations. The computation for \bar{v}_1 can be derived from Fig. B-1 by the following

$$\frac{\partial \bar{\omega}^x}{\partial p} + \bar{\nabla} \cdot \bar{W}^x = 0$$

(B-1)

$$\frac{\partial \bar{\omega}^x}{\partial p} + \frac{\partial \bar{v}_1}{\partial y} = 0$$

(B-2)

$$\frac{\bar{\omega}_2^x}{\Delta p} + \frac{\partial \bar{v}_1}{\partial y} = 0$$

(B-3)

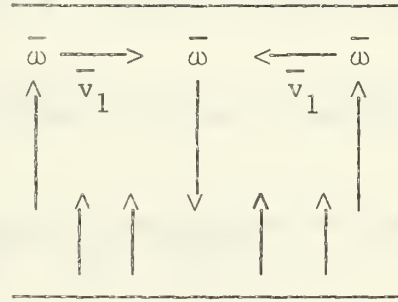


Fig. B-1

In finite difference form equation B-3 becomes

$$(\bar{v}_1)_1 \approx (\bar{v}_1)_i - \frac{\Delta y}{\Delta p} \left(\frac{(\bar{\omega}_2)_i + (\bar{\omega}_2)_{i+1}}{2} \right) \quad (B-4)$$

with $v_1 = 0.0$.

APPENDIX C - ENERGY TRANSFORMATION EQUATIONS

The following definitions are utilized in the energy transformation equations of Phillips [1956]

$$\text{Mean Potential Energy} \quad \bar{P} = \frac{u^2}{W} \int \left(\frac{\bar{\Psi}_1 - \bar{\Psi}_3}{2} \right)^2 dy \quad (C-1)$$

$$\text{Disturbance Potential Energy} \quad P' = \frac{u^2}{4W} \int (\Psi'_1 - \Psi'_3)^2 dy \quad (C-2)$$

$$\text{Mean Kinetic Energy} \quad \bar{K} = \frac{1}{4W} \int (\bar{u}_1^2 + \bar{u}_3^2) dy \quad (C-3)$$

$$\text{Disturbance Kinetic Energy} \quad K' = \frac{1}{2W} \int \left[\left(\frac{\partial \Psi'_1}{\partial x} \right)^2 + \left(\frac{\partial \Psi'_1}{\partial y} \right)^2 + \left(\frac{\partial \Psi'_3}{\partial x} \right)^2 + \left(\frac{\partial \Psi'_3}{\partial y} \right)^2 \right] dy \quad (C-4)$$

Phillips [1956] derived the following disturbance energy transformation equations which provide an excellent means for examining the extent to which the model contains the physical processes known to be important in the atmosphere.

$$[\bar{P} \cdot P'] = - \frac{u^2}{4W} \int \overline{v_1 (\Psi'_1 - \Psi'_3)} \frac{\partial}{\partial y} (\bar{\Psi}_1 - \bar{\Psi}_3) dy \quad (C-5)$$

$$[P' \cdot K'] = - \frac{f_o}{2p_2 W} \int \overline{\omega'_2 (\Psi'_1 - \Psi'_3)} dy \quad (C-6)$$

$$[K' \cdot \bar{K}] = - \frac{1}{2W} \int \left[\bar{u}_1 \frac{\partial}{\partial y} (\overline{u'_1 v'_1}) + \bar{u}_3 \frac{\partial}{\partial y} (\overline{u'_3 v'_3}) \right] dy \quad (C-7)$$

$$[K' \cdot A_H] = \frac{A_H}{2W} \int \left[(\zeta'_1)^2 + (\zeta'_3)^2 \right] dy \quad (C-8)$$

$$[K' \cdot A_v] = \frac{A_v}{2W} \int \overline{w'_3 \cdot w'_3} dy \quad (C-9)$$

The symbolic notation of the form $[\bar{P} \cdot P']$ for example, signifies a transformation of energy from one form - the first in the bracket - to the second form. The example $[\bar{P} \cdot P']$ represents the transformation of mean potential energy into the disturbance potential energy.

Utilizing equations (2.9), (2.10), (2.15) and (2.16), the components of the disturbance energy become

$$P' = \frac{\mu^2}{2W} \int_0^W (C^2 + D^2) dy \quad (C-10)$$

and

$$K' = \frac{1}{2W} \int_0^W \left[k^2 (A^2 + B^2 + C^2 + D^2) + \left(\frac{\partial A}{\partial y} \right)^2 + \left(\frac{\partial B}{\partial y} \right)^2 + \left(\frac{\partial C}{\partial y} \right)^2 + \left(\frac{\partial D}{\partial y} \right)^2 \right] dy \quad (C-11)$$

Similarly, equations (C-5) through (C-9) become

$$[\bar{P} \cdot P'] = - \frac{k\mu^2}{W} \int_0^W (BC - AD) \frac{\partial F}{\partial y} dy \quad (C-12)$$

$$[P' \cdot K'] = - \frac{1}{\Delta p W} \int_0^W [(WC) C + (WS) D] dy \quad (C-13)$$

$$[K' \cdot \bar{K}] = - \frac{k}{W} \int_0^W \left[\frac{\partial E}{\partial y} \left(B \frac{\partial^2 A}{\partial y^2} - A \frac{\partial^2 B}{\partial y^2} + D \frac{\partial^2 C}{\partial y^2} - C \frac{\partial^2 D}{\partial y^2} \right) + \frac{\partial F}{\partial y} \left(B \frac{\partial^2 C}{\partial y^2} - C \frac{\partial^2 B}{\partial y^2} + D \frac{\partial^2 A}{\partial y^2} - A \frac{\partial^2 D}{\partial y^2} \right) \right] dy \quad (C-14)$$

$$[K' \cdot A_H] = \frac{A_H}{W} \int_0^W \left\{ \left[\left(\frac{\partial^2}{\partial y^2} - k^2 \right) A \right]^2 + \left[\left(\frac{\partial^2}{\partial y^2} - k^2 \right) B \right]^2 + \left[\left(\frac{\partial^2}{\partial y^2} - k^2 \right) C \right]^2 + \left[\left(\frac{\partial^2}{\partial y^2} - k^2 \right) D \right]^2 \right\} dy \quad (C-15)$$

$$\begin{aligned}
 [K' \cdot A_v] = \frac{1}{2} \frac{A_v}{W} \int_0^W \left\{ k^2 \left[(A-C)^2 + (B-D)^2 \right] + \right. \\
 \left. \left[\left(\frac{\partial C}{\partial y} - \frac{\partial A}{\partial y} \right)^2 + \left(\frac{\partial D}{\partial y} - \frac{\partial B}{\partial y} \right)^2 \right] \right\} dy
 \end{aligned}
 \tag{C-16}$$

LIST OF REFERENCES

- Bryan, K., 1959: A numerical integration of certain features of the general circulation. Tellus 11, 163-174.
- Fultz, D. et al, 1959: Studies of thermal convection in a rotating cylinder with some implications for large scale atmospheric motions. Meteorological Monographs, Boston, American Meteorological Society, 4, 21, 104 pp.
- Hide, R., 1953: Some experiments on thermal convection in a rotating liquid. Quarterly Journal of the Royal Meteorological Society, 79, 161.
- Kuo, H. L., 1949: Dynamic instability of a two-dimensional non-divergent flow in a barotropic atmosphere. Journal of Meteorology, Vol. 6, 105-122.
- Kurihara, Yoshhio and J. L. Holloway, Jr., 1967: Numerical integration of a nine-level global primitive equation model formulated by the box method. Monthly Weather Review, Vol. 95, No. 8, 509-530.
- Kasahara, A. and W. M. Washington, 1967: NCAR global general circulation model of the atmosphere. Monthly Weather Review, Vol. 95, No. 7, 389-402.
- Lorenz, E. N., 1962: Simplified dynamic equations applied to the rotating-basin experiment. Journal of Atmospheric Sciences, 19, 39-51.
- Lorenz, E. N., 1963: The mechanics of vacillation. Journal of Atmospheric Sciences, 20, 448-464.
- Manabe, Syukuro, 1969: The atmospheric circulation and the hydrology of the earth's surface. Monthly Weather Review, Vol. 97, No. 11, 739-774.
- Manabe, Syukuro and J. Smagorinsky, 1967: Simulated climatology of a general circulation model with a hydrologic cycle: II. Analysis of the tropical atmosphere. Monthly Weather Review, Vol. 95, No. 4, 155-169.
- Matsuno, J., 1966: Numerical integrations of the primitive equations by a simulated backward difference method. Journal of Meteorological Society of Japan, 44, 76-84.
- Mintz, Y., 1965: Very long-term global integration of the primitive equations of atmospheric motion. WMO Technical Note No. 66, "WMO-IUGG Symposium on Research and Development Aspects of Long Range Forecasting, Boulder, Colo., 1964," Geneva, 1965, 141-167.

- Nitta, Takashi, 1967: Dynamical interaction between the lower stratosphere and the troposphere. Monthly Weather Review, Vol. 95, No. 6, 319-339.
- Phillips, N. A., 1956: The general circulation of the atmosphere. A numerical experiment. Quarterly Journal of the Royal Meteorological Society, Vol. 82, No. 352, 123-164.
- Richtmyer, R. D., 1957: Difference Methods for Initial Value Problems. Interscience Publishers, Inc., New York.
- Riehl, H., T. C. Yeh and N. E. LaSeur, 1950: A study of variations of the general circulation. Journal of Meteorology, Vol. 7, 181-194.
- Smagorinsky, J., 1963: General circulation experiments with the primitive equation, I. The basic experiment. Monthly Weather Review, Vol. 91, No. 3, 99-165.
- Smagorinsky, J., S. Manabe and J. L. Holloway, Jr., 1965: Numerical results from a nine-level general circulation model of the atmosphere. Monthly Weather Review, Vol. 93, No. 12, 727-768.
- Thompson, P. D., 1961: Numerical Weather Analysis and Prediction. The MacMillan Company, New York.
- Young, J. A., 1966: On the relation between zonal heating asymmetries and large-scale atmospheric fluctuations in space and time. Doctorate Thesis, Massachusetts Institute of Technology, Cambridge, Massachusetts.

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